

Vehicle Performance

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Road Loads

Exercise 1: Road Loads

Let's consider the following car

$$m = 1000 \, kg$$
 $\eta_t = 0.9$
 $S = 1.8 \, m^2$ $C_x = 0.31$ $\rho = 1.2 \, kg/m^2$
 $f = 0.01 \, + \, 10^{-5} \, V^2$



Compute the road loads generated at speed in between 0 and 50 m/s



Rolling resistance

$$F_{RR} = mg \cos \theta f_{RR} = mg \cos \theta (0.01 + 10^{-5} V^2)$$

It comes

$$V = 10 \, m/s$$
 $F_{RR} = 1000 \cdot 9,81 \cdot (0,01 + 10^{-5} \, 10^2) = 107,91 \, N$ $\mathcal{P}_{RR} = F_{RR} \, V = 1079,1 \, W$ $V = 25 \, m/s$ $F_{RR} = 1000 \cdot 9,81 \cdot (0,01 + 10^{-5} \, 25^2) = 159,91 \, N$ $\mathcal{P}_{RR} = F_{RR} \, V = 39971,75 \, W$ $V = 50 \, m/s$ $F_{RR} = 1000 \cdot 9,81 \cdot (0,01 + 10^{-5} \, 50^2) = 343,35 \, N$ $\mathcal{P}_{RR} = F_{RR} \, V = 17167 \, W$

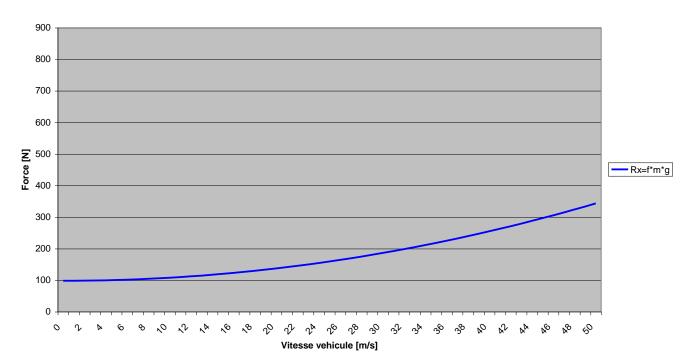
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Exercise 1: Road Loads

Rolling resistance

$$F_{RR} = mg \cos \theta f_{RR} = mg \cos \theta (0.01 + 10^{-5} V^2)$$

Resistance roulement





Aerodynamic drag

$$F_{AERO} = \frac{1}{2}\rho \, S \, C_x \, V^2$$

It comes

$$V = 10 \, m/s \qquad F_{AERO} = 0, 5 \cdot 1, 2 \cdot 1, 8 \cdot 0, 31 \cdot V^2 = 33, 48 \, N$$

$$\mathcal{P}_{AERO} = F_{AERO} \cdot V = 334, 8 \, W$$

$$V = 25 \, m/s \qquad F_{AERO} = 0, 5 \cdot 1, 2 \cdot 1, 8 \cdot 0, 31 \cdot 25^2 = 209, 25 \, N$$

$$\mathcal{P}_{AERO} = F_{AERO} \cdot V = 5231, 25 \, W$$

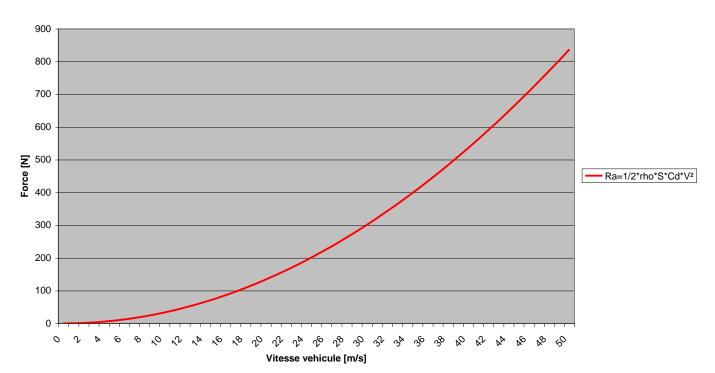
$$V = 50 \, m/s \qquad F_{AERO} = 0, 5 \cdot 1, 2 \cdot 1, 8 \cdot 0, 31 \cdot 50^2 = 837 \, N$$

$$\mathcal{P}_{AERO} = F_{AERO} \cdot V = 41850 \, W = 41,850 \, kW$$

Rolling resistance

$$F_{AERO} = \frac{1}{2} \rho \, S \, C_x \, V^2$$

Resistance aero





Total road resistance forces

$$F_{RES} = F_{RR} + F_{AERO} = mg (f_0 + f_2 V^2) \cos \theta + \frac{1}{2} \rho S C_x V^2$$

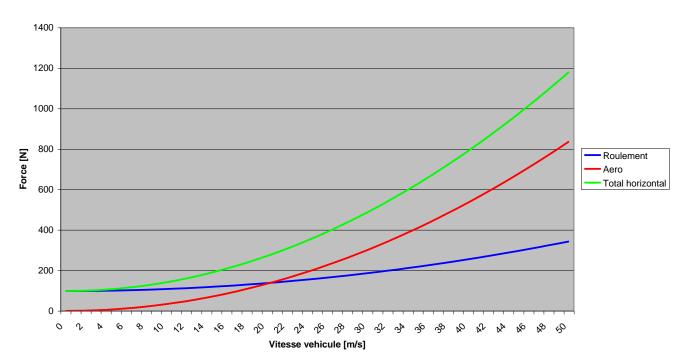
It comes

$$V = 10 \ m/s$$
 $F_{RR} + F_{AERO} = 107,91 + 33,48 = 141,39 \ N$ $\mathcal{P}_{RR} + \mathcal{P}_{AERO} = 1,4139 \ kW$ $V = 25 \ m/s$ $F_{RR} + F_{AERO} = 159,9 + 209,25 = 369,15 \ N$ $\mathcal{P}_{RR} + \mathcal{P}_{AERO} = 9,225 \ kW$ $V = 50 \ m/s$ $F_{RR} + F_{AERO} = 343,35 + 837 = 1180,35 \ N$ $\mathcal{P}_{RR} + \mathcal{P}_{AERO} = 59,0175 \ kW$

Total road resistance forces

$$F_{RES} = F_{RR} + F_{AERO} = mg (f_0 + f_2 V^2) \cos \theta + \frac{1}{2} \rho S C_x V^2$$

Force totale



Exercise 1: Road Loads

When aerodynamic drag and rolling resistance are equal?

$$F_{RR} = F_{AERO} \quad \iff \quad mg \left(f_0 + f_2 V^2 \right) \cos \theta = \frac{1}{2} \rho S C_x V^2$$

We have

$$\left(\frac{1}{2}\rho S C_x - mg f_2 \cos\theta\right) V^2 = mg f_0 \cos\theta$$

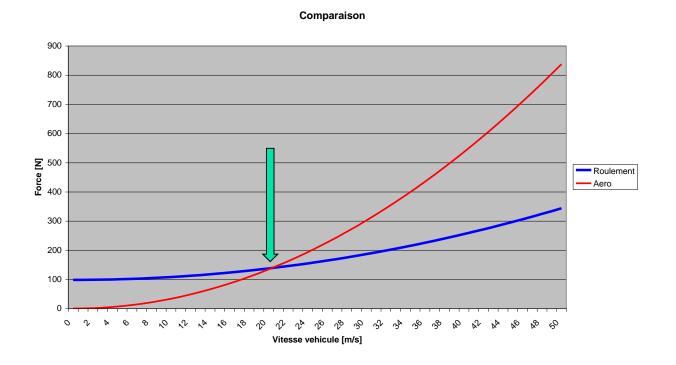
$$V = \sqrt{\frac{mg f_0 \cos\theta}{\frac{1}{2}\rho S C_x - mg f_2 \cos\theta}}$$

$$V = \sqrt{\frac{98,1}{0,2367}} = \sqrt{414,448} = 20,35 \ m/s = 73,29km/h$$



When aerodynamic drag and rolling resistance are equal?

$$F_{RR} = F_{AERO} \iff mg (f_0 + f_2 V^2) \cos \theta = \frac{1}{2} \rho S C_x V^2$$





Grading resistance

$$F_{GRADING} = mg \sin \theta$$

We have

$$slope = 3\% \qquad \Longleftrightarrow \qquad \tan\theta = 0,03$$

$$\iff \qquad \theta = 1,7183^{\circ}$$

$$\iff \qquad \sin\theta = 0,0299$$

$$\theta = 3\%$$
 $F_{GRADING} = mg \sin \theta$
= $1000 \cdot 9,81 \cdot 0,0299 = 294,3 N$

$$V = 10 \, m/s$$
 $\mathcal{P}_{GRAD.} = F_{GRAD.} \cdot V = 2,941 \, kW$ $V = 25 \, m/s$ $\mathcal{P}_{GRAD.} = F_{GRAD.} \cdot V = 7,3542 \, kW$ $V = 50 \, m/s$ $\mathcal{P}_{GRAD.} = F_{GRAD.} \cdot V = 14,7084 \, kW$

Exercise 1: Road Loads

Grading resistance

slope =
$$10\%$$
 \iff $\theta = 5,71^{\circ}$ \iff $\sin \theta = 0,0995$ $F_{GRADING} = 1000 \cdot 9,81 \cdot 0,0995 = 976,13 N$

slope =
$$20\%$$
 \iff $\theta = 11,3099^{\circ}$ \iff $\sin \theta = 0,1961$

$$F_{GRADING} = 1000 \cdot 9,81 \cdot 0,1961 = 1923,89 N$$

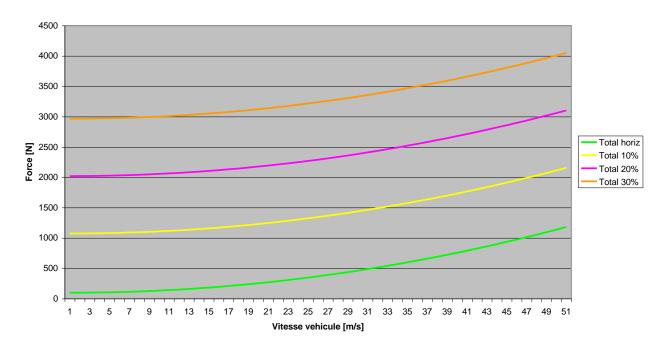
$$V = 10 \, m/s$$
 $\mathcal{P}_{GRAD.} = F_{GRAD.} \cdot V = 19,2389 \, kW$
 $V = 25 \, m/s$ $\mathcal{P}_{GRAD.} = F_{GRAD.} \cdot V = 48,0974 \, kW$
 $V = 50 \, m/s$ $\mathcal{P}_{GRAD.} = F_{GRAD.} \cdot V = 96,194 \, kW$

When aerodynamic drag and rolling resistance are equal?

$$F_{RES} = F_{RR} + F_{AERO} + F_{GRADING}$$

= $mg (f_0 + f_2 V^2) \cos \theta + \frac{1}{2} \rho S C_x V^2 + mg \sin \theta = A + B V^2$

Force totale



Exercise 2: Shell Eco Marathon

Let's consider the following car

$$m = 145 kg$$
 $f = 0.01$
 $S = 0.95 m^2$ $C_x = 0.28$ $\rho = 1.22 kg/m^2$



- Compute the road loads generated at speed V=8,33 m/s (30 km/h)
 - On level road
 - When θ =2,1°

Exercise 2: Shell Eco Marathon

Rolling resistance

$$F_{RR} = mg \cos \theta f_{RR}$$

$$= 145 \cdot 9,81 \cdot 1 \cdot 0,01 = 14,2245 N$$

$$\mathcal{P}_{RR} = F_{RR} \cdot V = 14,2245 \cdot 8,33 = 118,4900 W$$

Aerodynamic resistance

$$F_{AERO} = \frac{1}{2} \rho S C_x V^2$$

$$= 0, 5 \cdot 1, 22 \cdot 0, 95 \cdot 0, 28 \cdot 8, 33^2 = 11, 2590 N$$

$$\mathcal{P}_{AERO} = F_{AERO} \cdot V = 11, 2590 \cdot 8, 33 = 93, 7878 W$$

Road resistance

$$F_{RES} = F_{RR} + F_{AERO} = 14,2245 + 11,2590 = 25,4835 N$$

 $\mathcal{P}_{RES} = \mathcal{P}_{RR} + \mathcal{P}_{AERO} = 118,49 + 93,7878 = 212,2779 W$



Grading resistance

$$\theta = 2, 1^{\circ} \quad \sin \theta \simeq \tan \theta = 3,6643 \ 10^{-2}$$

$$F_{GRADING} = mg \sin \theta$$

$$= 145 \cdot 9,81 \cdot \sin 2, 1^{\circ} = 52,1238 \ N$$

■ Rolling resistance → negligible modification!

$$\cos \theta = \cos 2, 1^{\circ} = 0,9993$$

$$F_{RR} = mg \cos \theta f_{RR}$$

$$= 145 \cdot 9,81 \cdot 0,9998 \cdot 0,01 = 14,2149 N$$

Road resistance

$$F_{RES} = F_{RR} + F_{AERO} + F_{GRADE} = 25,4835 + 52,1238 = 77,6073 N$$

If V=8,33 m/s

$$\mathcal{P}_{RES} = F_{RES} \cdot V = 77,6073 \cdot 8,33 = 646,4688 \ W$$

Let's consider the following car

$$m = 180 \, kg$$
 $f = 0,0018$ (Data: Michelin)
 $S = 1,049 \, m^2$ $C_x = 0,20$ $\rho = 1,22kg/m^2$





- Compute the road loads generated at speed V=26 km/h
 - On level road
 - When θ = 0,35° and θ = 2%



Speed :

$$V = 26km/h = 26/3, 6 = 7,23 \, m/s$$

Slope:

$$\theta = 0,35^{\circ} = 6,10 \ 10^{-3} \ rad$$
$$\cos 0,35^{\circ} = 0,9999 \quad \sin 0,35^{\circ} = 6,1086 \ 10^{-3}$$

And

$$2\% \iff \arctan(0,02) = 1,1457^{\circ}$$

$$\cos 1,1457^{\circ} = 0,9998 \quad \sin 1,1457^{\circ} = 19,9949 \ 10^{-3}$$

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Exercise 2: Shell Eco Marathon

Rolling resistance

$$F_{RR} = mg \cos \theta \ f_{RR} = 180 \cdot 9,81 \cdot 1,0 \cdot 0,0018 = 3,1784 \ N$$

 $\mathcal{P}_{RR} = F_{RR} \cdot V = 3,1794 \cdot 7,23 = 22,9801 \ W$

Aerodynamic resistance

$$F_{AERO} = \frac{1}{2} \rho S C_x V^2$$

$$= 0, 5 \cdot 1, 22 \cdot 1, 049 \cdot 0, 20 \cdot 7, 23^2 = 6,8761 N$$

$$\mathcal{P}_{AERO} = F_{AERO} \cdot V = 6,8761 \cdot 7, 23 = 49,7143 W$$

Road resistance

$$F_{RES} = F_{RR} + F_{AERO} = 3,1784 + 6,8761 = 10,0545 N$$

 $\mathcal{P}_{RES} = \mathcal{P}_{RR} + \mathcal{P}_{AERO} = 22,9801 + 49,7143 = 72,6940 W$

Exercise 2: Shell Eco Marathon

Grading resistance

$$\theta = 2\%$$
 $\theta = 1,1457^{\circ}$ $\sin \theta = 1,9996 \cdot 10^{-2}$

$$F_{GRADING} = mg \sin \theta$$

$$= 180 \cdot 9,81 \cdot 0,019996 = 35,316 N$$

- Rolling resistance → negligible modification!
- Road resistance

$$F_{RES} = F_{RR} + F_{AERO} + F_{GRADE} = 25,4835 + 52,1238 = 77,6073 N$$

 $\mathcal{P}_{RES} = F_{RES} \cdot V = 77,6073 \cdot 7,23 = 328,0287 W$



If the vehicle is equipped with two electric motors of the following characteristics

$$C_{max} = 0,9743 \ N.m$$

 $i = 8,2$ $R_e = 0,2737 \ m$
 $\eta_{GearBox} = 0,9875$ $\eta_{Bearings} = 0,98$

- What is the net force available?
- What is the maximum slope that be overcome?
- What is the maximum acceleration?

Exercise 2: Shell Eco Marathon

- What is the net force available?
 - Transmission efficiency

$$\eta_t = \eta_{gear} \, \eta_{bearings} = 0,9875 \cdot 0,98 = 0,96775$$

Tractive force generated by one motor

$$F_t^{(1)} = \eta \frac{i}{R_e} C_{max} = 0,96775 \frac{8,2}{0,2737} 0,9743 = 28,2638 N$$

Net available tractive force

$$F_{net} = 2 \cdot F_t^{(1)} - F_{RES} = 2 \cdot 28,2658 - 10,0945 = 46,4371 N$$



What is the maximum slope that be overcome?

$$F_{GRADE} = mg \sin \theta_{max} = F_{net} = F_t - F_{RES}$$

$$\sin \theta_{max} = \frac{F_{net}}{mg} = \frac{F_t - F_{RES}}{mg}$$

$$= \frac{46,4371}{180 \cdot 9,81} = 2,6298 \cdot 10^{-2}$$

$$\theta_{max} = 2,6\%$$



What is the maximum acceleration?

$$m\frac{dV}{dt} = F_{net} = F_t - F_{RES}$$

$$a_{max} = \frac{F_{net}}{m} = \frac{F_t - F_{RES}}{m}$$

$$= \frac{46,4371}{180} = 0,2579 \, m/s^2$$

 Determine the road resistance of a semi trailer truck when traveling at the cruise speed of V=90 km/h

$$m = 40000 \ kg$$
 $f_{RR} = 0.0085$
 $S = 10 \ m^2$ $C_x = 0.64$
 $\eta_t = 0.90$



- Grade resistance on a 3% road.
- Which slope can be overcome at 90 km/h if the truck is equipped with a 335 kW engine (Mercedes-Benz OM470)?

 Determine the road resistance of a semi trailer truck when traveling at the cruise speed of V=90 km/h

Truck type	C _d	Source	
(1)	(2)	(3)	
Single unit	0.70	Fitch [1994]	
Tractor-semitrailer	0.70	Fitch [1994]	
Car hauler - cattle hauler	0.96 – 1.10	SAE J2188	
Garbage	0.95 - 1.05	SAE J2188	
No aerodinamic aids	0.78	SAE J2188	
Aerodinamic aids on roof	0.64	SAE J2188	
Full aerodinamic treatment	0.58	SAE J2188	



Exercise 3: Road Resistance of a Truck

Speed :

$$V = 90km/h = 90 \cdot 1000/3600 = 25.0 \, m/s$$

Rolling resistance

$$F_{RR} = mg \cos \theta f_{RR}$$

$$= 40000 \cdot 9.81 \cdot 1 \cdot 0.0085 = 3335.40 N$$

$$\mathcal{P}_{RR} = F_{RR} \cdot 25.0 = 83.385 kW$$

Aerodynamic drag

$$F_{AERO} = \frac{1}{2} \rho S C_x V^2$$

$$= 0, 5 \cdot 1, 2 \cdot 10.0 \cdot 0.64 \cdot 25^2 = 2400 N$$

$$\mathcal{P}_{AERO} = F_{AERO} \cdot V = 2400 \cdot 25 = 60.0 kW$$



Total road resistance on level road

$$F_{RES} = F_{RR} + F_{AERO} = 5735.4 N$$

 $\mathcal{P}_{RES} = \mathcal{P}_{RR} + \mathcal{P}_{AERO} = 83.385 + 60.0 = 143.385 \ kW$

Ratio between rolling resistance and aerodynamic drag

$$\frac{\mathcal{P}_{RR}}{\mathcal{P}_{AERO}} = \frac{83.385}{60.0} = 1.3898$$

Power need at the engine

$$\mathcal{P}_{mot} = \frac{\mathcal{P}_{RES}}{\eta_t} = \frac{143.385}{0.9} = 159.51 \, kW$$

$$\mathcal{P}_{mot} = \frac{159.51}{0.736} = 216.46 \, HP$$



For which speed aerodynamic drag is equal to the rolling resistance

$$F_{RR} = F_{AERO} \iff mg f_{RR} = \frac{1}{2} \rho S C_x V^2$$

$$V = \sqrt{\frac{mg f_{RR}}{\frac{1}{2} \rho S C_x}} = \sqrt{\frac{40000 \cdot 9.81 \cdot 0.0085}{\frac{1}{2} \cdot 1.2 \cdot 10 \cdot 0.64}}$$

$$= 29.4719 \ m/s = 106.0989 \ km/h$$



Determine net power available and max slope that can be taken

$$\mathcal{P}_{RR} + \mathcal{P}_{AERO} + \mathcal{P}_{GRADE} = \eta_t \, \mathcal{P}_{max}$$

$$83385 + 60000 + mg \sin \theta \, V = 0.9 \cdot 335000$$

$$\sin \theta = \frac{0.9 \cdot 335000 - 143385}{40000 \cdot 9.81 \cdot 25} = 0.0161$$

Maximum slope at 90 km/h is 1.61%





 Let's consider the following vehicle BMW Z3 (model 2000)

$$m = 1295 \ kg$$

 $C_x = 0.37$ $S = 2.24 \ m^2$
 $f = 0.0136 + 0.4E - 7 \ V^2[km/h]$

Tire 225/50 R 16

$$P_{max} = 118 \ HP$$
 $\omega_{nom} = 5500 \ rpm$ $C_{max} = 180 \ N.m$ $\omega_{Cmax} = 3900 \ rpm$

	1	2	3	4	5
i_g	4.23	2.52	1.66	1.22	1.00
i_d			3.38		





Exercise 4

- Determine missing parameters
- Define approximations of power and torque curves of the engine
- Compute the road resistance forces and draw their evolution from 0 to 200 km/h
- Compute the tractive forces for the five gear ratios and draw the diagram of tractive forces and road resistance of the vehicle



Exercise 4

- Let's estimate the missing parameters
- Rolling radius

Tire
$$225/50 R 16$$

$$D = 16 \cdot 25, 6 + 2 \cdot 0, 50 \cdot 225 = 631.40 mm$$

$$R_e \simeq 0.98 \cdot D/2 = 309, 38 mm$$

- Transmission efficiency
 - Engine with longitudinal mounting
 - Driven at rear axle
 - Manuel transmission with dry friction clutch
 - One direct drive gear ratio (5)

$$\eta_t(1, 2, 3, 4) = 1.00,9875^2 \ 0.975 = 0.95$$

$$\eta_t(5) = 1.01.00.975 = 0.975$$

Exercise 4: Power curve approximations

Let's find an approximation of the power curves

$$P_1 = P_{max} = 118 \ HP = 118 \cdot 736 = 86.84 \ kW$$

 $P_1 = P_{max} = 86840 \ W$ $\omega_1 = \omega_{nom} = 5500 \ rpm$
 $C_2 = C_{max} = 180 \ N.m$ $\omega_2 = \omega_{Cmax} = 3900 \ rpm$

$$\omega_1 = 5500 \frac{2\pi}{60} = 575,9587 \, rad/s$$
 $\omega_2 = 408,4070 \, rad/s$
$$\mathcal{P}(\omega_2) = \mathcal{P}_2 = C_{max} \, \omega_{C_{max}}$$
$$= 180 \cdot 408,4070 = 75.513 \, kW$$

$$\mathcal{P}_2/\mathcal{P}_1 = 0.84654$$
$$\omega_2/\omega_1 = 0.70909$$

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Power approximation

One looks for a power function of the type

$$\mathcal{P} = \mathcal{P}_1 - a |\omega - \omega_1|^b$$
 with $b > 0$

It comes

$$b = \frac{\frac{\omega_1}{\omega_2} - 1}{\frac{\mathcal{P}_1}{\mathcal{P}_2} - 1} = 2.2631$$
 $a = \frac{\mathcal{P}_1 - \mathcal{P}_2}{|\omega_1 - \omega_2|^b} = 0.12340$

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Polynomial approximation

Polynomial approximation of order 3

$$\mathcal{P}(\omega)/\mathcal{P}_1 = a_0 + a_1 (\omega/\omega_1) + a_2 (\omega/\omega_1)^2 + a_3 (\omega/\omega_1)^3$$

Identification of the coefficients

$$a_{0} = 0$$

$$a_{1} + a_{2} + a_{3} = 1$$

$$a_{1} + a_{2} + a_{3} = 0$$

$$a_{1} + a_{2} + a_{3} = 0$$

$$a_{2} + 2 + a_{3} = 0$$

$$a_{2} + 2 + a_{3} = 0$$

$$a_{1} = 0.042187$$

$$a_{2} = 3.248236$$

$$a_{3} = -2.290423$$



Polynomial approximation

Polynomial approximation of order 4

$$\mathcal{P}(\omega)/\mathcal{P}_1 = a_0 + a_1 (\omega/\omega_1) + a_2 (\omega/\omega_1)^2 + a_3 (\omega/\omega_1)^3 + a_4 (\omega/\omega_1)^4$$

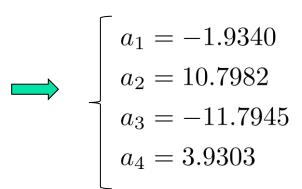
Solution of the linear system

$$a_1 + a_2 + a_3 + a_4 = 1$$

$$a_1 + 2 a_2 + 3 a_3 + 4 a_4 = 0$$

$$a_1 n_2 + a_2 n_2^2 + a_3 n_2^3 + a_4 n_2^4 = \mathcal{P}_2/\mathcal{P}_1$$

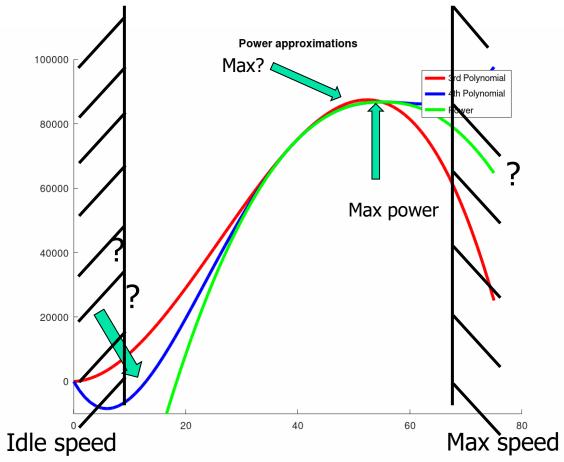
$$a_2 + 2 a_3 n_2 + 3 a_4 n_2^2 = 0$$





Comparison of Power approximations

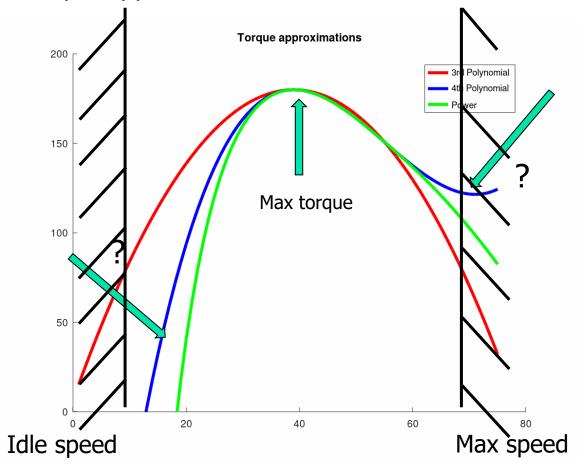
Power approximations





Comparison of Torque approximations

Torque approximations



Road resistance

Rolling resistance

$$F_{RR} = mg \cos \theta f_{RR}$$

$$f_{RR} = 0.0136 + 0.4E - 7 V^{2} [km/h]$$

$$f_{0} = 0.0136$$

$$f_{2} = 0.4E - 7 (3.6)^{2} = 5.184E - 7 [V \text{ in } m/s]$$

Aerodynamic drag

$$F_{AERO} = \frac{1}{2} \rho S C_x V^2$$

$$= 0.5 \cdot 1,22 \cdot 2.24 \cdot 0.37 \cdot V^2$$

$$= 0.5056 V^2 [N]$$



Road resistance

Grading resistance

$$F_{GRADING} = mg \sin \theta$$

Road resistance

$$F_{RES} = F_{RR} + F_{AERO} + F_{GRADE}$$

$$= mg \cos \theta (f_0 + f_2 V^2) + 1/2\rho SC_x V^2 + mg \sin \theta$$

$$F_{RES} = A + B V^2$$

$$A = mg \cos \theta f_0 + mg \sin \theta$$

$$B = 1/2\rho S C_x + mg \cos \theta f_2$$

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Road resistance

If $\theta = 0\%$

$$A = mg f_0 = (1295 + 75) \cdot 0.81 \cdot 0.0136 = 182.78 N$$

$$B = 1/2\rho S C_x + mg \cos \theta f_2$$

$$= 0.5 \cdot 1.22 \cdot 2.24 \cdot 0.37 + 1370 \cdot 9.81 \cdot 5.184 \cdot 10^{-7}$$

$$= 0.50425$$

• If θ =3%

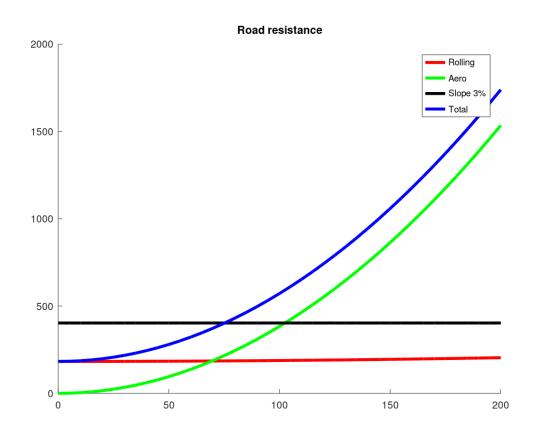
$$F_{GRADING} = \Delta A = mg \sin \theta$$

= 1370 · 9.81 · 0.03 = 403.1910

```
% Force at wheels
                                                      % FRES = A + B V**2
vup=200.;
                                                      ares = m*grav*frr0*cos(theta) + m*grav*sin(theta)
vlow=0.;
                                                      bres = 0.5*rho*S*Cx + m*grav*frr2*cos(theta)
                                                      Fres= ares + bres*vms.^2:
v=vlow:5:vup;
vms = v/3.6:
                                                      FRLT= m*grav*frr0*cos(theta) + m*grav*frr2*cos(theta)*vms.^2;
                                                      FAERO = 0.5*rho*S*Cx*vms.^2:
% Road resistance
                                                      % 3% = 1.7184 degres
                                                      theta = pi*1.7184/180.;
% Re 0.309
                                                      FGRAD = m*grav*sin(theta)*ones(length(vms),1);
fRR = f0 + f2 V**2
% f0 = 0.0136
                                                      figure
f2 = 0.4E-7 * (3.6)**2 = 5.184E-7
                                                      hold on
% S = 2.24 m^{2}
                                                      plot(v, FRLT, 'LineWidth', 3, 'Color', 'red')
% Cx = 0.37
% eta tranmission: 0.95 (moteur longitudinal avant) plot(v,FAERO,'LineWidth',3,'Color','green')
                                                      plot(v, FGRAD, 'LineWidth', 3, 'Color', 'black')
                                                      plot(v, Fres, 'LineWidth', 3, 'Color', 'blue')
m = 1295.+75.;
                                                      ylim([0 2000])
grav=9.81;
                                                      title('Road resistance')
Re = 0.309;
                                                      legend('Rolling', 'Aero', 'Slope 3%', 'Total')
frr0 = 0.0136:
                                                      hold off
frr2 = 5.184e-7:
rho=1.2;
S = 2.24;
Cx = 0.37;
```

Road resistance

Plot the road resistance from v=0 to 200 km/h





Tractive forces

- Let's now plot the tractive forces for the different gear ratio
 - Speed in terms of the engine rotation speed

$$v = \omega_e \, \frac{R_e}{i}$$

Tractive force in terms of the engine speed and torque value

$$F_t = \eta_t \, \frac{i}{R_e} \, C(\omega_e)$$

$$R_e = 0.3090$$
 $\eta_t(1, 2, 3, 4) = 1.00,9875^2 \ 0.975 = 0.95$ $\eta_t(5) = 1.01.00.975 = 0.975$

	1	2	3	4	5
i_g	4.23	2.52	1.66	1.22	1.00
i_d	3.38				
$i = i_g i_d$	14.2974	8.5176	5.6108	4.1236	3.38

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```
%
    Tractive forces
%
    Gear box: il=4.23 / i2 = 2.52 / i3 = 1.66 / i4 = 1.22 / i5 = 1.0
% Differential : id= 3.38
id = 3.38;
il = 4.23*id;
i2 = 2.52*id;
i3 = 1.66*id;
i4 = 1.22*id;
i5 = 1.00*id;
%
etatrans = 0.95;
etatransdirect = 0.975;
%
NROT=1000:100:6000;
%
```

```
NROT=1000:100:6000;
for i=1:length(NROT)
   omega = NROT(i)*pi/30.;
   Pcal = P1*(A3_0 + A3_1*(omega/O1) + A3_2*(omega/O1).^2 + A3_3*(omega/O1).^3);
   Ccal = Pcal/omega;
   vmsl(i)=3.6*omega*Re/il;
   FT1(i) = etatrans*i1*Ccal/Re;
   vms2(i)=3.6*omega*Re/i2;
   FT2(i) = etatrans*i2*Ccal/Re;
   vms3(i)=3.6*omega*Re/i3;
   FT3(i) = etatrans*i3*Ccal/Re;
   vms4(i)=3.6*omega*Re/i4;
   FT4(i) = etatrans*i4*Ccal/Re;
   vms5(i)=3.6*omega*Re/i5;
   FT5(i) = etatransdirect*i5*Ccal/Re;
 end
```

```
figure
hold on
plot(v,Fres,'LineWidth',3,'Color','black')
plot(vms1,FT1,'LineWidth',3,'Color','red')
plot(vms2,FT2,'LineWidth',3,'Color','magenta')
plot(vms3,FT3,'LineWidth',3,'Color','green')
plot(vms4,FT4,'LineWidth',3,'Color','cyan')
plot(vms5,FT5,'LineWidth',3,'Color','blue')
ylim([0 10000])
title('Tractive Forces')
legend('Road Resistance','Gear 1','Gear 2','Gear 3','Gear 4','Gear 5')
hold off
```

Tractive forces

■ Plot the tractive force from v=0 to 200 km/h

