MECA0527: PERFORMANCE & DESIGN OF BATTERY ELECTRIC VEHICLES

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Performances of Electric Vehicles

- Vehicle driving performance is assessed by
 - Acceleration time
 - Maximum speed
 - Gradeability
- In EV drivetrain design: the motor power rating and the transmission parameters are selected to meet the performance specifications
- They depend mostly on the speed-torque characteristics of the traction motor

Traction motor characteristics



- At low speed: constant torque
 - Voltage supply increases with rotation speed through electronic converter while flux is kept constant
- At high speed: constant power
 - Motor voltage is kept constant while the flux is weakened,
 - Torque is reduced hyperbolically with the rotation speed
- Base speed: transition speed from constant torque to constant power regime

Traction motor characteristics



 Speed ratio X = ratio between maximum rotation speed to base speed

$$X = \frac{\omega_{max}}{\omega_B}$$

- X ~ 2 Permanent Magnet motors
- X ~ 4 Induction motors
- X ~ 6 Switched Reluctance motors

For a given power, a longer constant power region (large X) gives rise to an important max constant torque, and so high vehicle acceleration and gradeability. Thus the transmission can be simplified.

Tractive efforts and transmission requirement

Remind traction effort and vehicle speed

$$F_t = \eta_t \frac{C_m i}{R_e} \qquad \qquad v = \frac{\omega_m R_e}{i}$$

- The use of multi-gear or single gear transmission depends on the motor speed-torque characteristics.
 - For a given rated power, a long constant power region makes possible to use a single gear transmission, because of the high tractive efforts at low speeds.
 - For long constant torque plateau and a given rated power, the available maximum torque is sometimes not sufficient so that a multi gear is generally preferred.

Tractive efforts and transmission requirement

- For a low x (x=2) motor, tractive effort is not large enough and 3-gear transmission may be chosen.
- For intermediate x=4, a twogear transmission should be preferred.
- For a large x=6, a single gear transmission is possible.
- The 3 designs have the same tractive force / speed profiles, and so the same acceleration and gradeability performance.



Ehsani et al. Fig 5.5. Low x (x=2) e-motor and 3-gear transmission

Tractive efforts and transmission requirement



and 2-gear transmission

(SRM) and single gear transmission

EV max speed



 Max speed can be evaluated by calculating the intersection between the tractive force curve and the resistance curve or alternatively the tractive power (constant) and the resistance forces power.

 $\eta_t P_m^{max} = A V_{max}^{max} + B (V_{max}^{max})^3$

 Then we can define the gear ratio of the transmission so that max speed is reached at the motor max rotation speed

$$i^{opt} = \frac{\pi N_m^{max} R_e}{30 V_{max}^{max}}$$

9

EV max speed





 However sometimes, the intersection between the max power and the resistance power does not happen at V_{max}^{max}

$$\eta_t P_m^{max} = A V_{max}^{max} + B (V_{max}^{max})^3$$

This is the case when the V_{max} is prescribed

$$\bar{V}_{max} = \frac{\pi N_m^{max} R_e}{30 i} < V_{max}^{max}$$

Or when the gear ratio is given

$$V_{max} = \frac{\pi \ N_m^{max} \ R_e}{30 \ \overline{i}} < V_{max}^{max}$$

Gradeability of EV



Check also nonslip condition

$$F_t \le \mu W_f \qquad F_t \le \mu W_r$$

 Gradeability is ruled by the net tractive force available

$$F_t^{net} = F_t - F_{RR} - F_{aero}$$
$$= F_t - mgf\cos\theta - 0,5\ \rho\ SC_x\ V^2$$

The maximum grade that can be overcome at a given speed is:

$$\sin \theta = \frac{F_t - F_{RR} - F_{aero}}{mg} = \frac{F_t^{net}}{mg}$$

It comes :

$$\sin \theta = \frac{d - f\sqrt{1 + f^2 - d^2}}{1 + f^2}$$

$$d = (F_t - F_{aero})/mg$$

Gradeability of EV

The maximum slope can be evaluated as follows

$$F_t - F_{aero} - F_{RR} - mg\sin\theta = 0$$
$$\iff F_t - F_{aero} - mg\cos\theta f - mg\sin\theta = 0$$

If we set

$$d = (F_t - F_{aero})/mg$$

It comes :

$$d - \sin \theta = f \, \cos \theta$$
$$(d - \sin \theta)^2 = f^2 \, \cos^2 \theta$$
$$\iff d^2 - 2d \sin \theta + \sin^2 \theta = f^2 (1 - \sin^2 \theta)$$
$$\iff (1 + f^2) \, \sin^2 \theta - 2d \, \sin \theta + (d^2 - f^2) = 0$$



• It a second order equation in $\sin\theta$ $(1 + f^2) \sin^2 \theta - 2d \sin \theta + (d^2 - f^2) = 0$

Solving for sinθ gives

$$\sin \theta = \frac{2d \pm \sqrt{4d^2 - 4(1+f^2)(d^2 - f^2)}}{2(1+f^2)}$$
$$= \frac{d \pm \sqrt{d^2 - d^2 + f^2 - f^2 d^2 + f^4}}{1+f^2}$$
$$= \frac{d \pm \sqrt{f^2 - d^2 f^2 + f^4}}{1+f^2} = \frac{d \pm f \sqrt{1 - d^2 + f^2}}{1+f^2}$$

It comes :

$$\sin \theta = \frac{d - f\sqrt{1 + f^2 - d^2}}{1 + f^2}$$

Gradeability of EV



$$\sin \theta = \frac{d - f\sqrt{1 + f^2 - d^2}}{1 + f^2}$$

$$d = (F_t - F_{aero})/mg$$

 One can increase the tractive force by increasing the transmission gear ratio i

$$F_t = \eta C_m^{max} \frac{i}{R_e}$$

 However, increasing the reduction ratio is reducing the maximum speed (green line → blue line)

$$V_{max} = \omega_{max} \frac{R_e}{i}$$

- It is also positive for the acceleration (see after)
- Verify that adherence is not saturated

$$F_t \le \mu W_{f/r}$$

- Acceleration can be evaluated by the time to accelerate from a given low speed (often zero) to a given high speed (e.g. 100 km/h).
- Acceleration performance is often more important for drivers than max speed and gradeability
- Acceleration performance dictates the motor power rating!



Newton second law:

$$F_t - \sum F_{res} = F_{net} = m_e \frac{dV}{dt}$$

 Effective mass me to account for the inertia of the wheel, the axle, the transmission, and the electric machine J

$$m_e = \gamma m$$

$$\gamma = 1. + (I_w/R_e^2) + (J_m/R_e^2) i^2 \simeq 1.04 + (J_m/R_e^2) i^2$$

Time to accelerate from 0 to V_f:

$$\Delta t_{0 \to V_f} = \int_0^{V_f} \frac{m_e}{F_{net}(v)} dv = \int_0^{V_f} \frac{m_e}{F_t(v) - mgf - 1/2\rho S C_x v^2} dv$$

Tractive force expression of EV

$$F_t = \eta_t \; \frac{C_m \; i}{R_e}$$

Below the base speed

$$\omega \in [0, \omega_B] \quad C = C^{max}$$

$$C = C^{max} = \frac{P^{max}}{\omega_B}$$



$$F_t = \eta_t \frac{P^{max} i}{\omega_B R_e} = \eta_t \frac{P^{max}}{v_B} = \frac{P^{max}_t}{v_B} = \text{Cste}$$
$$v_B = \frac{\omega_B R_e}{i} \qquad P^{max}_t = \eta_t P^{max}$$

17

Tractive force expression of EV

$$F_t = \eta_t \; \frac{C_m \; i}{R_e}$$

• Over the base speed

$$\omega \in [\omega_B, \omega_{max}] \quad P = P^{max}$$





$$F_t = \eta_t \frac{P^{max} i}{\omega_m R_e} = \eta_t \frac{P^{max}}{v} = \frac{P_t^{max}}{v}$$
$$v = \frac{\omega_m R_e}{i} \qquad P_t^{max} = \eta_t P^{max}$$

18



 Acceleration time can be calculated by the integral

$$t_{a} = \int_{0}^{V_{b}} \frac{\gamma m}{P_{t}/V_{b} - mgf - 0, 5\rho SC_{x}V^{2}} \, dV \\ + \int_{V_{b}}^{V_{f}} \frac{\gamma m}{P_{t}/V - mgf - 0, 5\rho SC_{x}V^{2}} \, dV$$

Approximation solution: neglect the rolling and the drag resistances

$$t_a = \frac{\gamma m}{2P_t} (V_f^2 + V_b^2)$$

 Let's calculate the acceleration time when neglecting the aerodynamic and rolling resistance

$$\begin{split} t_{acc} &= \int_{0}^{V_{b}} \frac{\gamma m}{P_{t}/V_{b}} \, dV + \int_{V_{b}}^{V_{f}} \frac{\gamma m}{P_{t}/V} \, dV \\ t_{acc} &= \int_{0}^{V_{b}} \frac{\gamma m \, V_{b}}{P_{t}} \, dV + \int_{V_{b}}^{V_{f}} \frac{\gamma m \, V}{P_{t}} \, dV \\ &= \frac{\gamma m \, V_{B}}{P_{t}} \, [V]_{0}^{V_{B}} + \frac{\gamma m}{P_{t}} \, \left[\frac{V^{2}}{2}\right]_{V_{b}}^{V_{f}} \\ &= \frac{\gamma m}{P_{t}} \left(V_{b}^{2} + \frac{V_{f}^{2} - V_{b}^{2}}{2}\right) \\ &t_{acc} &= \frac{\gamma m \, V_{f}^{2} + V_{b}^{2}}{2} \end{split}$$



- Sizing of rated power of electric motor:
 - If the acceleration time is given:

$$P_{max} = \frac{\gamma m}{2 t_a \eta_t} (V_f^2 + V_b^2)$$

 However, to determine more accurately the rated power, one can add a correction that is <u>the average power dissipated by the</u> <u>resistance forces during the acceleration phase</u>

$$\bar{P}_{aver}^{Res} = \frac{1}{t_a} \int_0^{t_a} mgf \, V + 0, 5\rho S C_x V^3 \, dt$$

$$P_{max} = \frac{\gamma m}{2 t_a \eta_t} (V_f^2 + V_b^2) + \bar{P}_{aver}^{Res}$$

 To compute the average power dissipation by the rolling and aerodynamic resistances during the acceleration, one generally assumes that it is performed at constant power all along the acceleration (actually it is only the case over V_B)

$$F = m \frac{dV}{dt} \qquad \qquad F = \frac{P}{V}$$

It comes

$$\frac{P}{V} = m\frac{dV}{dt} \quad \Longrightarrow \quad dt = \frac{m}{P}V \, dV$$

$$t_2 = \int_{t_1=0}^{t_2} dt = \int_{V_1=0}^{V_2} \frac{m}{P} V dV = \frac{m}{2P} (V_2^2 - V_1^2) = \frac{m}{2P} V_2^2$$

Inserting into the integral,

$$V(t) = V_f \sqrt{\frac{t}{t_a}}$$

It comes the estimated power of the motor

$$\begin{split} \bar{P}_{aver}^{Res} &= \frac{1}{t_a} \int_0^{t_a} mgf \, V(t) + 0, 5\rho S C_x V(t)^3 \, dt \\ &= \frac{1}{t_a} \int_0^{t_a} mgf \, V_f \left(\frac{t}{t_a}\right)^{1/2} + 0, 5\rho S C_x V_f^3 \left(\frac{t}{t_a}\right)^{3/2} \, dt \\ &= \frac{1}{t_a} \left\{ mgf \, \frac{2}{3} \, \frac{t_a^{3/2}}{t_a^{1/2}} \, V_f + 0, 5\rho S C_x \frac{2}{5} \frac{t_a^{5/2}}{t_a^{3/2}} \, V_f^3 \right\} \\ &= mgf \, \frac{2}{3} \, V_f + \frac{1}{5} \rho S C_x \, V_f^3 \end{split}$$



- Power rating of the e-machine to ensure a given acceleration time
 - Inertia forces

$$P_{max} = \frac{\gamma m}{2 t_a \eta_t} (V_f^2 + V_b^2)$$

Average power dissipated by resistance forces4

$$\bar{P}_{aver}^{Res} = \frac{2}{3}mgfV_f + \frac{1}{5}\rho SC_x V_f^3$$

Estimated power of the motor

$$P_t = \frac{\gamma m}{2t_a} (V_f^2 + V_b^2) + \frac{2}{3} mgfV_f + \frac{1}{5} \rho SC_x V_f^3$$



- The result shows that for a given acceleration performance, lower vehicle base speeds will result in smaller motor power rating
- However, the power rating decline rate to the vehicle base speed reduction is not identical

$$\frac{dP_t}{dV_b} = \frac{\gamma m}{t_a} V_b$$

Eshani Fig 5.9



 Fine estimation of acceleration time requires solving exactly (numerically) the Newton equation

$$t_a = \int_0^{V_f} \frac{\gamma m}{F_t - mgf - 0, 5\rho S C_x V^2} \, dV$$



Eshani Fig 5.10







- 1D system with one electric motor connected to the mechanical load via a gear box or reduction ratio r
 - M mass of load (here the vehicle)
 - J inertia of electric motor
 - $i = Z_1/Z_2$, the gear ratio
 - R_e: tire rolling radius
 - r= Re/I transmission length
 - a:=dv/dt acceleration of the load (vehicle)

Newton equation of the vehicle

$$\int \int \int \frac{1}{|z|^2} = Z_2/Z_1$$

$$R_e$$

$$M, \omega_r$$

 J, ω_m

$$F_t = M \frac{dV}{dt}$$

Tractive force

$$F_t = \eta \frac{i}{R_e} \left(C_m - J_m \frac{d\omega_m}{dt} \right)$$

 Relation between engine rotation speed and velocity

$$V = \frac{\omega_m R_e}{i}$$

Equation of motion

$$\eta \frac{i}{R_e} \left(C_m - J_m \frac{i}{R_e} \frac{dV}{dt} \right) = M \frac{dV}{dt}$$

Newton equation of the vehicle



 J, ω_m

$$C_m = \left(\frac{J_m}{(R_e/i)} + M(R_e/i)\right) \frac{dV}{dt}$$
$$= \left(M + J(i/R_e)^2\right) (R_e/i) \frac{dV}{dt}$$

Acceleration

$$a = \frac{dV}{dt}$$

Acceleration

$$a = \frac{C_m \left(i/R_e\right)}{M + J \left(i/R_e\right)^2}$$

Derivative of acceleration with respect to gear ratio

$$\frac{\partial a}{\partial (i/R_e)} = \frac{C_m}{M + J(i/R_2)^2} - \frac{C_m(i/R_e)}{(M + J(i/R_e)^2)^2} \, 2(i/R_e)J = 0$$

- Optimal gear ratio $(i/R_e)^{opt} = \sqrt{\frac{M}{J}}$
- Optimal acceleration power

$$a^{max} = \frac{1}{2} \frac{C_m}{\sqrt{JM}} = \frac{1}{2} \frac{C_m}{M} (i/R_e)^{opt}$$

 Conclusion: this is the maximum acceleration that can be given to the load by a motor with maximum torque C_m.



- Driving cycle V(t) is given
- Evaluate the acceleration required: differentiating the velocity profile:

$$\frac{dV}{dt} \simeq \frac{V(t_{k+1}) - V(t_k)}{t_{k+1} - t_k}$$

 Tractive force is given by the net force necessary to follow the driving cycle

$$F_t = mgf\cos\theta + \frac{1}{2}\rho SC_x SV^2 + \gamma m\frac{dV}{dt}$$

Eshani et al. Fig 5.12 Speed profile and tractive effort in FT75 drive cycle



Eshani et al. Fig 5.12 Speed profile and tractive effort in FT75 and US06 drive cycle



Eshani et al. Fig 5.12 Speed profile and tractive effort in FT75 HW and J227a driving cycle ³³



Eshani et al. Fig 5.12 Speed profile and tractive effort in J227a schedule C/D drive cycle



Eshani et al. Fig 5.13 Time distribution on vehicle speed and tractive effort in FT75 drive cycle

- In transportation the unit of energy is usually the kWh (kiloWatt hour) (preferred to J ou kJ)
 - ICE with liquid fuels: L/100 km or mpg
 - Gaseous fuel (CH₄, H₂): kg/100 km
- Advantage: size of batteries given in kWh at battery ports so that the driving range can be calculated immediately.
- Energy consumption results from the time integration of the power output and input at battery terminal.

- Energy power output
 - Equal to the resistance power and the power losses in the transmission and motor drive including the power electronic loses

$$P_{bat}^{out} = \frac{V}{\eta_t \eta_m(C_m, \omega_m)} \left(mgf\cos\theta + mg\sin\theta + \frac{1}{2}\rho SC_x V^2 + \gamma m\frac{dV}{dt} \right) > 0$$

 The non traction loads are not included (auxiliary loads) while they can be significant, and they should be added to the traction load.



Eshani et al. Fig 5.14 Typical electric motor efficiency characteristics

- The efficiency of the traction motor varies with the operating points on the speed-torque (speed-power) plane
- Good design: large overlap between the maximum efficiency region and the region visited by the most frequent operation points

• The regenerative braking power at battery can be evaluated as

$$P_{bat}^{in} = \alpha \eta_t \eta_m V \left(mgf\cos\theta + mg\sin\theta + \frac{1}{2}\rho SC_x V^2 + \gamma m\frac{dV}{dt} \right) < 0$$

- In which
 - road slope sin θ <0 and/or deceleration dV/dt<0
 - 0<α<1 is the fraction of energy recovered during braking
 The braking factor α is a function of the applied braking strength and the design and control of braking system

Typical α is around 0,3

• The net energy consumption from batteries is:

$$En^{out} = \oint_{P_t>0} P_{bat}^{out} dt - \oint_{P_t<0} P_{bat}^{in} dt$$

- When the net battery energy consumption reaches the total energy in the batteries, measured at terminal, the batteries are empty and need to be charged.
- The traveling distance between two charges is called the effective travel range.
- It is dependent on the battery capacity, the road resistance power, the driving cycle, the effectiveness of regenerative braking, the efficiency of the car and its powertrain.

Preliminary design procedure of EV

 First estimate the rating power of the e-motor. Acceleration time is generally the most critical criterion

$$P_{max} = \frac{\gamma m}{2 \eta_t t_a} (V_f^2 + V_b^2) \qquad V_b = V_{max} / X$$

- V_b can be estimated using N_{max} and the aspect ratio of the selected e-motor technology (X factor)
- Then a reduction ratio of the transmission can be determined using the target top speed

$$i = \frac{2\pi N_m^{max} R_e}{60 V_{max}}$$

Select one motor from the catalog

Check the top speed

$$\eta_t P_m^{max} = A V_{max} + B V_{max}^3$$

And the grade ability

$$\sin \theta = \frac{d - f\sqrt{1 - d^2 + f^2}}{1 + f^2} \qquad d = (F_t - F_{Aero})/mg$$

 If not satisfied, adapt the gear ratio i and if necessary, select a second gear ratio to satisfy both specifications

Adapt the base speed

$$V_b = \frac{2\pi N_m^{max} R_e}{60 \ i \ X}$$

Compute a finer estimation of the acceleration power

$$P_t = \frac{\gamma m}{2t_a} (V_f^2 + V_b^2) + \frac{2}{3} mgfV_f + \frac{1}{5} \rho S C_x V_f^3$$

 And solve numerically the time integration of the Newton's second law to quote the acceleration time

$$t_a = \int_0^{V_f} \frac{\gamma m}{F_t - mgf - 0, 5\rho S C_x V^2} \, dV$$

- Repeat the design cycle till convergence
- Use simulation to estimate energy consumption and size the battery pack to reach the desired range
- Select the relevant driving cycles

$$\begin{split} P_{bat}^{out} &= \frac{V}{\eta_t \eta_m(C_m, \omega_m)} \left(mgf\cos\theta + mg\sin\theta + \frac{1}{2}\rho SC_x V^2 + \gamma m \frac{dV}{dt} \right) \\ P_{bat}^{in} &= \alpha \; \frac{V}{\eta_t \eta_m} \left(mgf\cos\theta + mg\sin\theta + \frac{1}{2}\rho SC_x V^2 + \gamma m \frac{dV}{dt} \right) \\ En^{out} &= \oint_{P_t > 0} P_{bat}^{out} dt - \oint_{P_t < 0} P_{bat}^{in} dt \end{split}$$

EV Inverse dynamics





